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HOSTETTER PAPER

The paper of Susan Hostetter, "Measuring Income for Developing and Reviewing Individual Tax Law Changes: Alternative Concepts," explores the problem of what to measure from an administratively based statistical system in order to provide the most effective information for the analysis of policy and as a statistical representation of income in the United States. The careful presentation of concepts and comparison of their implications will surely be of interest to many who use these data.

I am reminded of a sentence in Thomas Pynchon's *Gravity's Rainbow*: "Roger is only a statistician." I have recalled this sentence on occasion when asked to discuss a well-presented analysis of primarily substantive content. Except for complementing the author on this work, I am unable to add to what she has accomplished. A paper of this sort represents an important resource to the statistical public, and I am pleased that it was included in this session.

AUGER PAPER

The next paper, "Family Data from the Canadian Personal Income Tax File," by Edouard Auger, takes the problem of using administrative data for statistical purposes in a different direction: use of tax data to approximate census concepts in Canada. The census concept of family is one of great substantive importance but also some challenge to derive from these records. The results the paper reports appear quite encouraging, and the careful work it represents is exemplary.

The paper does not consider in detail what would seem to be the next step in the process: the development of models to adjust the tax data further to increase comparability of the results with the census concepts. I presume such work will be considered. I think that the direction represented by the paper, namely to investigate carefully improvements and adjustments to the tax data, is the correct first step to take before resorting to models. I wish the author continued success in his research.

HINIKER PAPER

The paper of John P. Hiniker, "The Selection of Returns for Audit by the IRS," represents a solution to the "cocktail party problem," namely how does a statistician describe the profession to someone with limited exposure to statistical analyses? The general solution to this problem usually takes the form of interesting examples, and the selection of IRS returns for audit certainly commands interest. The paper effectively illustrates application of statistical concepts in a practical setting.

The basic approach is sound. To add to the scope of the paper, however, I will mention some possible different analyses that could be considered for this or similar problems.

The method described in the paper, discriminant analysis, was derived from an original assumption that a vector of characteristics, $x = \{x_i\}$, followed a normal distribution with mean m_g and variance V , for observations from group g . As long as the group means differ from each other, a discriminant function in the form of a linear function or functions (in the case of more than two groups) of the components of x , can be used to classify the membership in the groups. This function can be estimated from sample data from observations for which group membership is known. Under these assumptions, the sample means for each group and the pooled estimate of the within-group covariance matrix, V , are sufficient statistics for the linear discriminant function.

Logistic regression is also related to the problem of classification. In the simplest case, logistic regression represents a model of the form

$$\ln \frac{P(g=1; x)}{P(g=2; x)} = b_0 + b_1x_1 + b_2x_2 + \dots$$

No restrictions are required on the distribution of x , but maximum likelihood estimation of the parameters of this model generally requires iteration.

Under the assumptions of linear discriminant analysis just described, the logarithm of the ratio of group probabilities, conditional on the observed x , can be shown to have the form of the logistic regression model. Because of the more specialized assumptions of discriminant analysis, the form of maximum likelihood estimator differs from that for logistic analysis, but the two problems have a close underlying connection.

The paper acknowledges the inappropriateness of the underlying assumptions of discriminant analysis for these data, but makes reference to the general robustness of this approach in motivating its application. In my view, this position is reasonable. As a direction for possible future research, however, the logistic model bears investigation.

The paper describes use of likelihood ratios in the development of the classification model; log likelihood ratios are a more appropriate choice for this problem, since the solution would then become invariant under reordering of group membership, unlike the current version. With this modification, the problem becomes closely connected to the Fellegi-Sunter procedure considered in the paper by Drew, Armstrong, and Dibbs. [2]

The two-stage procedure represents a practical adaptation rather than a necessary consequence of the general theory for the classification problem. Its apparent effect is to compensate for lack of fit of the first model in the region of key interest, namely, returns with a high probability of revision from audit. This sort of evidence suggests that improvements in the model may be possible through a different formulation.

It is usually easier to think of additional models for a set of data than to implement them

and make them work. Consequently, I will add to the preceding remarks my appreciation of the careful and creative effort in developing and implementing the models and presenting them in this session.

OH-SCHEUREN PAPER

The paper "Osculatory Interpolation Revisited" has both aesthetic and methodological merit. The authors, H. Lock Oh, and Fritz Scheuren, succeed at making this potentially obscure (although clearly important!) topic lively and interesting. The geometric interpretation is both pretty and useful for generating new variations and insights.

As a discussant, I can find nothing to add to the treatment of the problem the authors discuss directly. Consequently, a few tangential observations follow.

The paper discusses the problem for highly accurate counts, based on complete enumerations or very large samples. Additional technical issues may arise when sampling error is a significant consideration, and this issue may represent a direction for possible future research.

The paper also considers administrative data that are presumably essentially free from rounding effects. The use of the additional information represented by the means within the inter-

vals, which is advantageous in the problem considered in the paper, may be less clearly helpful in the presence of substantial rounding effects. This question should be considered by researchers considering application of these methods to income data reported by respondents in surveys.

ACKNOWLEDGMENT

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FOOTNOTES

- [1] The views expressed are attributable to the author and do not necessarily reflect those of the Census Bureau.
- [2] Drew, Douglas J.; Armstrong, John B., and Dibbs, M. Ruth. (1987) "Research into a Register of Residential Addresses for Urban Areas of Canada," 1987 American Statistical Association Proceedings, Section on Survey Research Methods.